

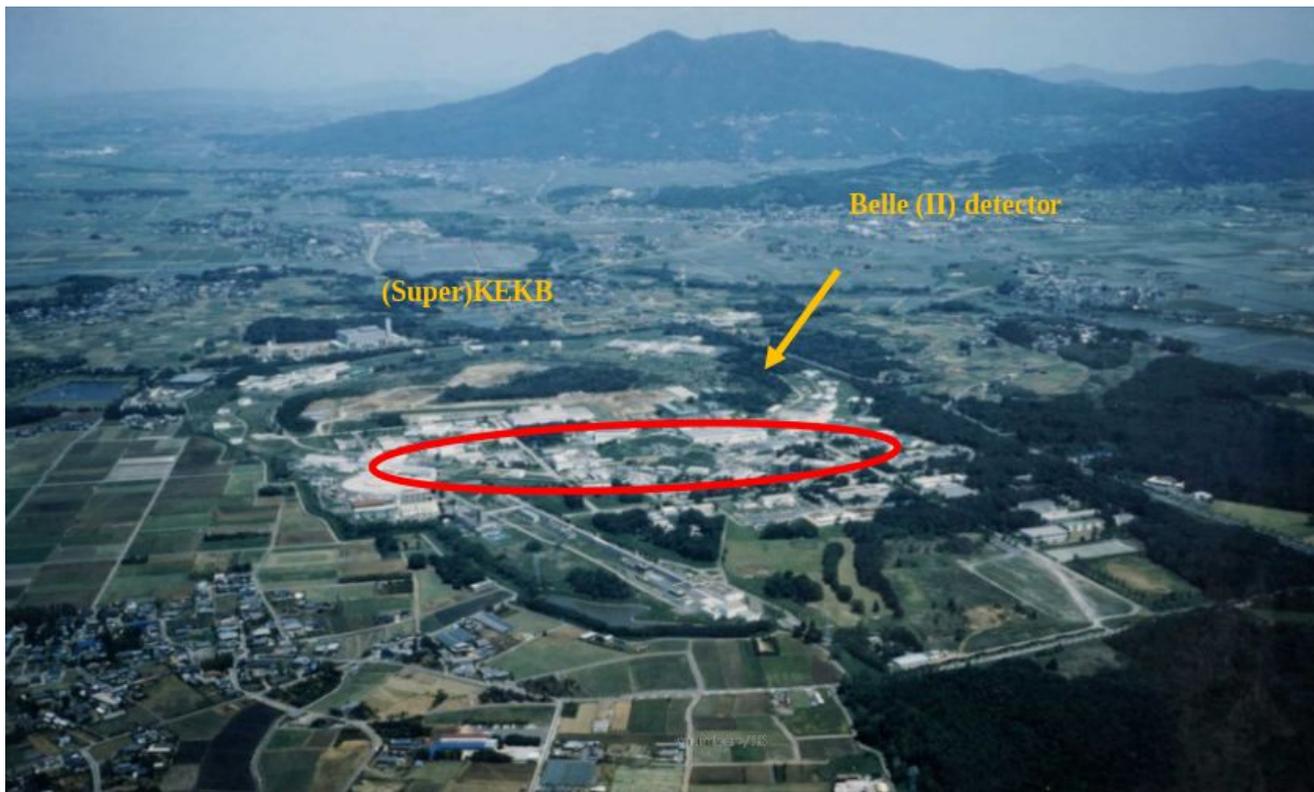
# Prospects for Measurement of the Dijet Transverse Momentum Decorrelation Spectrum at Belle II

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Jet Physics: from RHIC/LHC to EIC  
2022-07-01

# Agenda

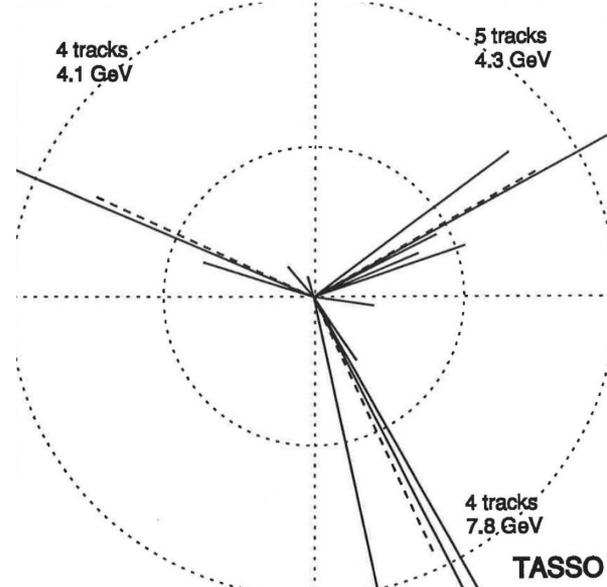
- Introduce Belle / Belle II experiment
- Previous jet measurement at Belle
- Unique opportunity for QCD studies at Belle II
- Advantages of the Belle II detector and its event shapes
- Show how Belle II can help understand QCD, hadronization, nonperturbative effects
- Show how polarization can be accessed in  $e^+e^-$  collisions without beam polarization

# KEK facility



# QCD and jet physics in $e^+e^-$ collisions

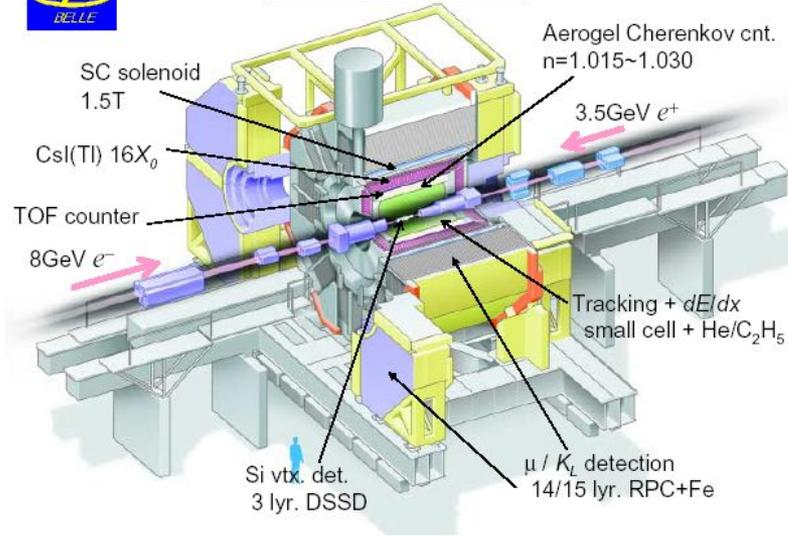
- Has long history in studying QCD
  - e.g. PETRA at DESY: discovery of the gluon (1979)



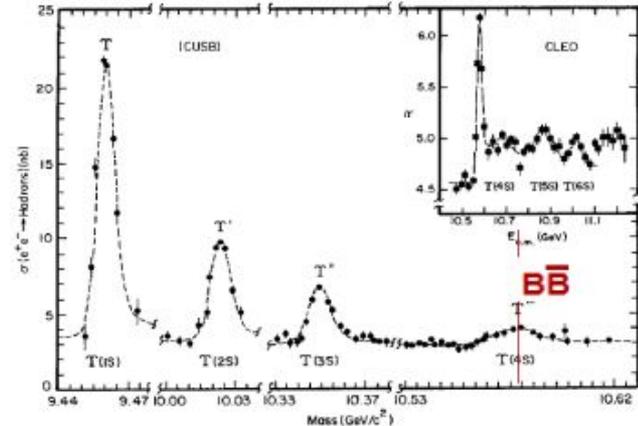
# Belle Experiment (1999 - 2010)



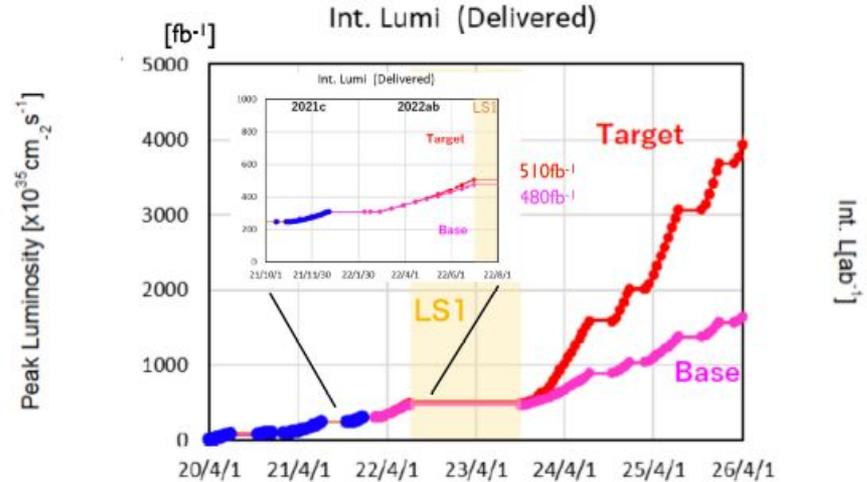
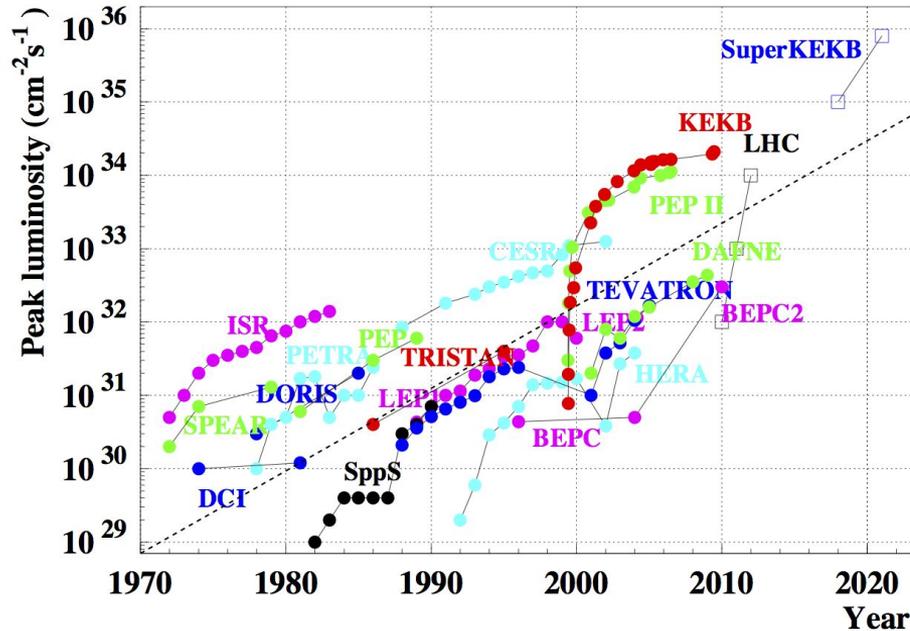
## Belle Detector



Exp.	Scans / Off-res. $\text{fb}^{-1}$	$\Upsilon(5S)$		$\Upsilon(4S)$		$\Upsilon(3S)$		$\Upsilon(2S)$		$\Upsilon(1S)$	
		10876 MeV $\text{fb}^{-1}$	0.1 $10^6$	10580 MeV $\text{fb}^{-1}$	17.1 $10^6$	10355 MeV $\text{fb}^{-1}$	5 $10^6$	10023 MeV $\text{fb}^{-1}$	10 $10^6$	9460 MeV $\text{fb}^{-1}$	21 $10^6$
CLEO	17.1	0.4	0.1	16	17.1	1.2	5	1.2	10	1.2	21
BaBar	54	$R_b$ scan		433	471	30	122	14	99	—	
Belle	100	121	36	711	772	3	12	25	158	6	102



# The next-generation B-factory: SuperKEKB

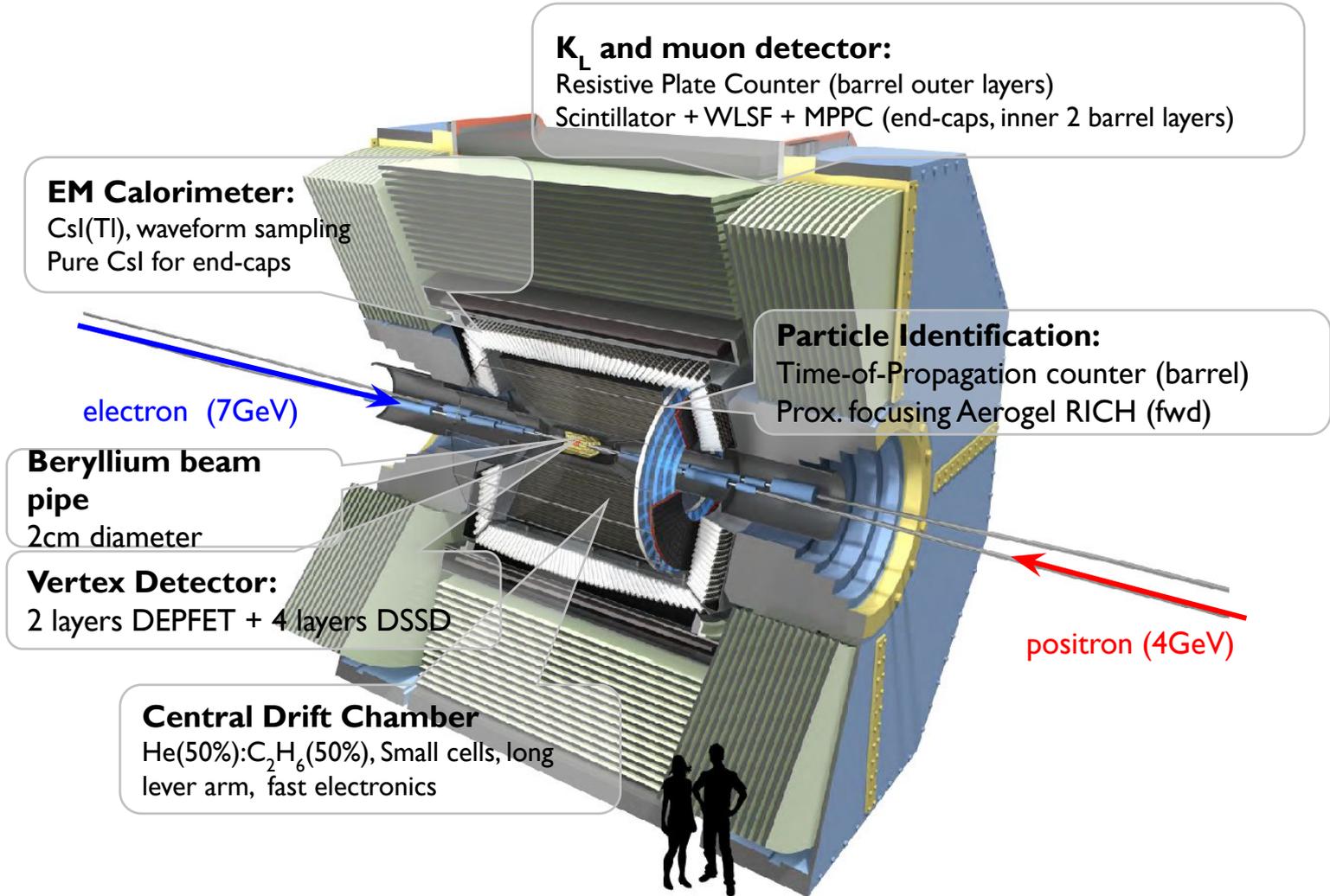


Beam currents *only* a factor of two higher than KEKB (~PEPII)

"nano-beams" are the key; vertical beam size is 50nm at the IP

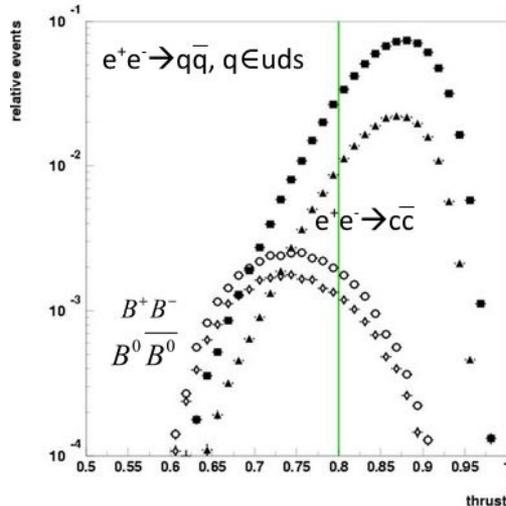
- World record luminosity
- Expecting 50 x Belle integrated luminosity (100 x BaBar)

# Belle II



# How to use a B-factory for jet physics?

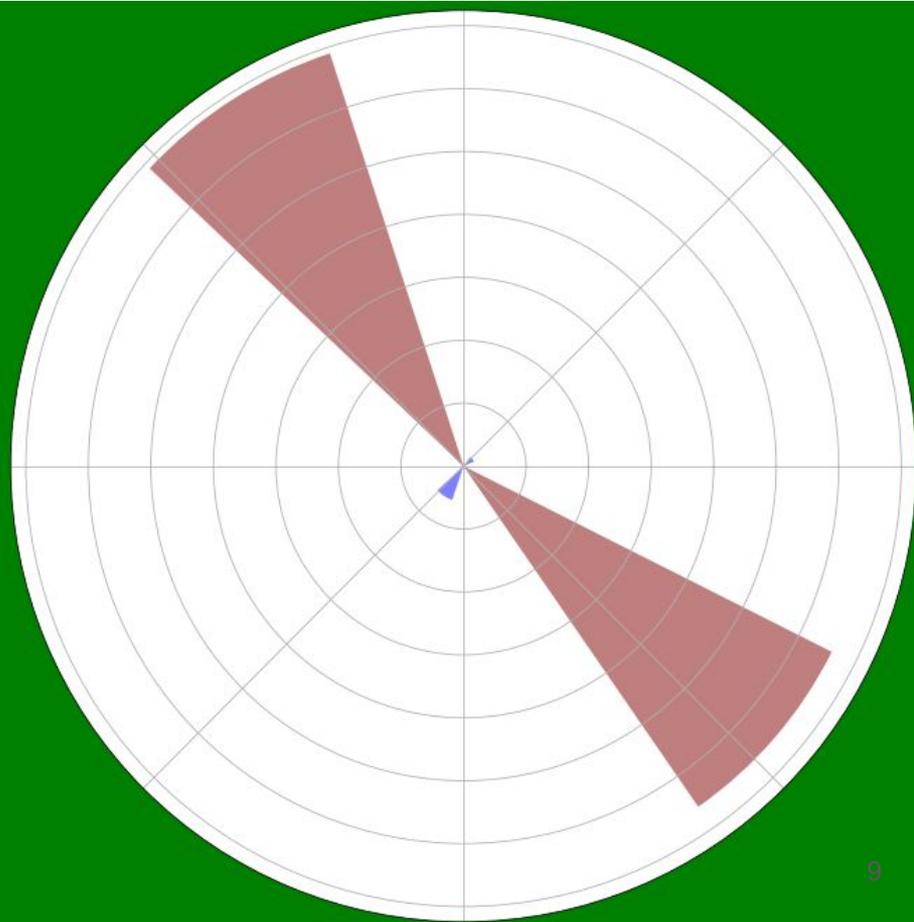
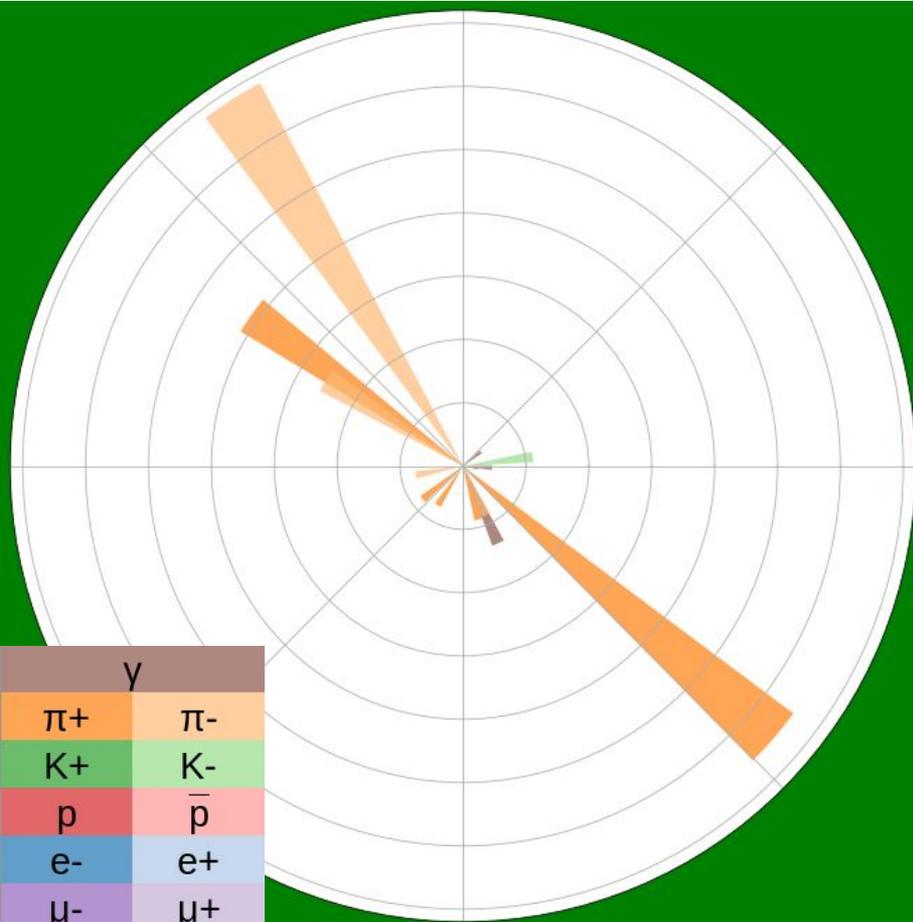
- Shapes of different event types are key
- Since they are produced at  $Y(4S)$ , the  $B\bar{B}$  events are very spherical
- Meanwhile  $q\bar{q}$  events tend to form high-thrust dijet events
- Cuts on thrust or related properties provide clean  $q\bar{q}$  dijet event sample



$$\text{Thrust} : T = \frac{\sum_i |p_i \cdot \hat{n}|}{\sum_i |p_i|}$$

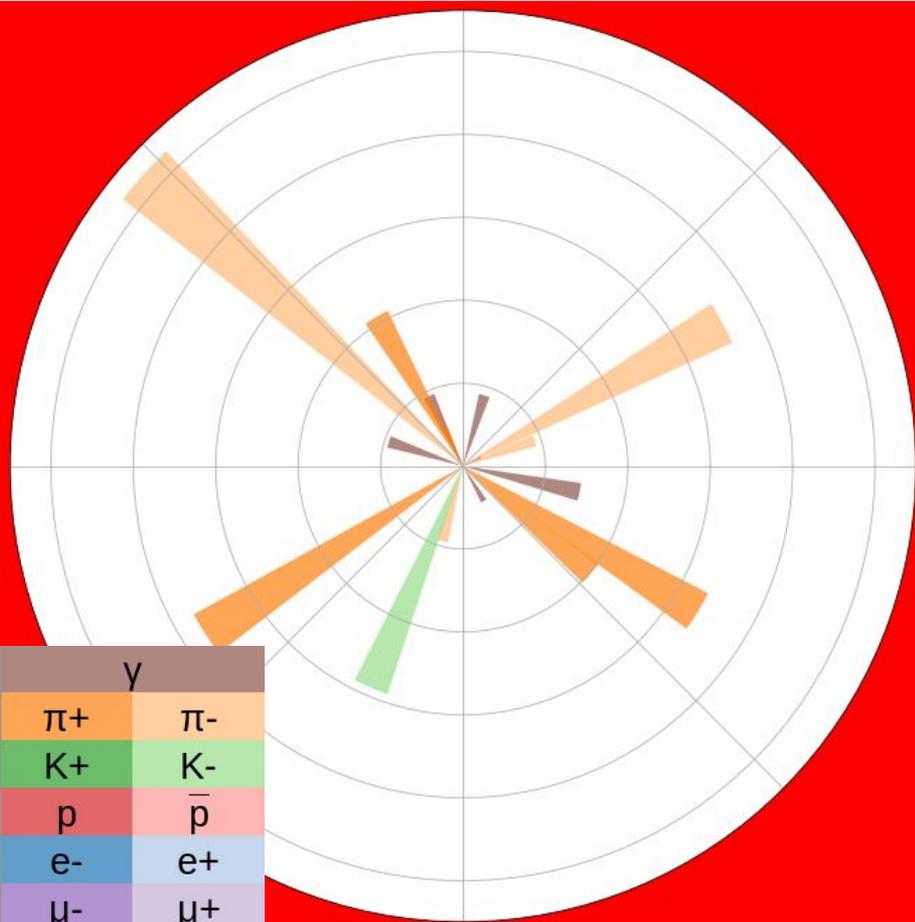
Particles

Jets

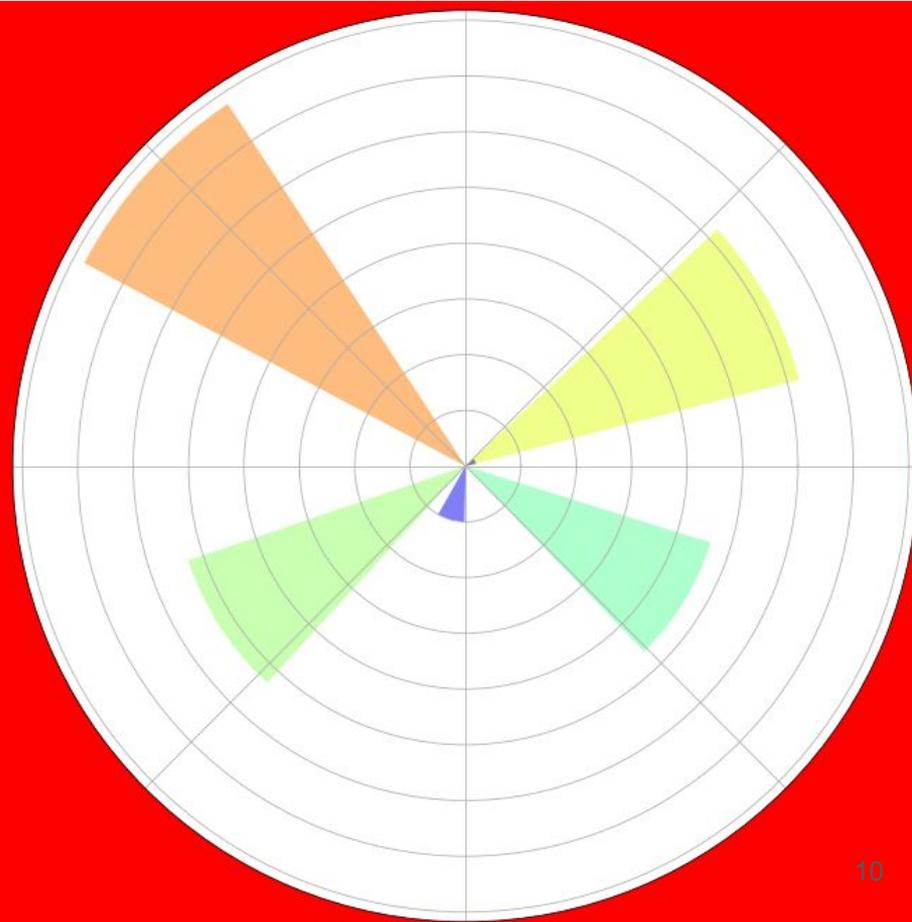


$\gamma$	
$\pi^+$	$\pi^-$
$K^+$	$K^-$
$p$	$\bar{p}$
$e^-$	$e^+$
$\mu^-$	$\mu^+$

Particles

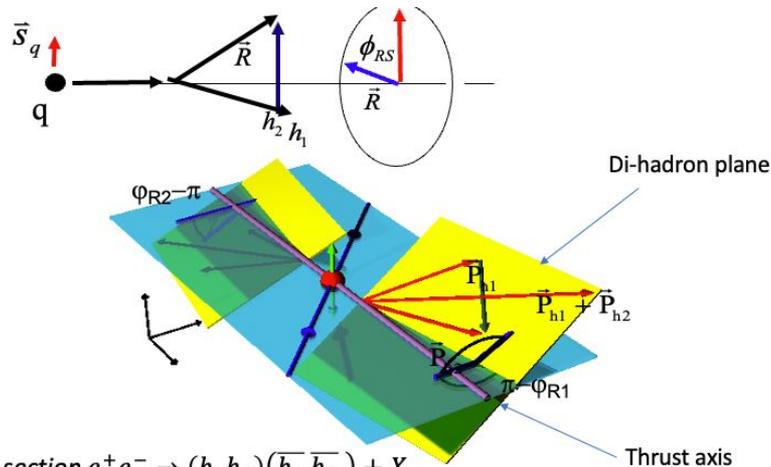


Jets



# How to study spin-dependent effects with unpolarized beams?

- Key: use that the  $q$  and  $\bar{q}$  spins are correlated
  - close to 100% transversal polarisation in barrel
- This allows to then access quantities like e.g.  $G_1^\perp$  (c.f. 1505.08020 [hep-ex])



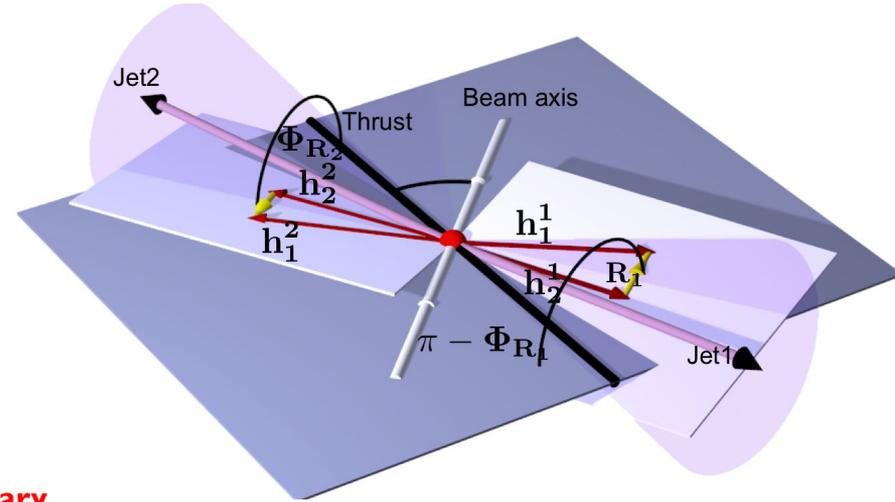
Cross-section  $e^+e^- \rightarrow (h_1 h_2)(\bar{h}_1 \bar{h}_2) + X$   
 $\propto D_1^\perp D_1^\perp + H_1^\perp H_1^\perp \cos(\phi_{R1} + \phi_{R2})$

- Statistics Hungry, only possible at B-factories

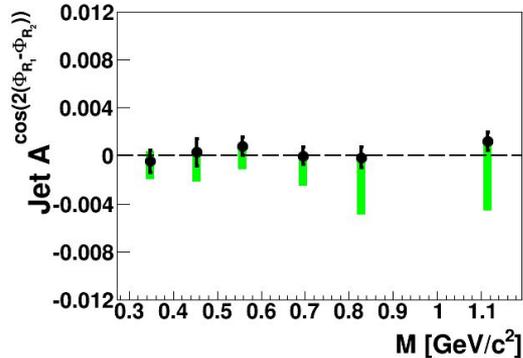
# Jet physics results from Belle

## Asymmetries for $\text{Cos}(2(\varphi_{R1}-\varphi_{R2}))$ ( $G_1^\perp$ )

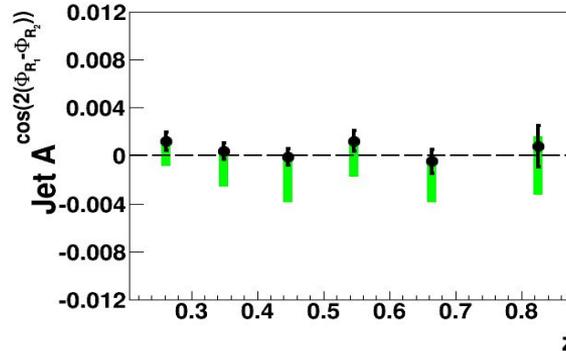
- The asymmetry turned out to be projected  $\equiv 0$
- Result showcases good control of systematic uncertainties possible in this type of measurement at Belle



**Belle Preliminary**



**Belle Preliminary**



1505.08020 [hep-ex]

# What possibilities does this open?

- Clean events and good PID capabilities
- Can get good samples of quark-jets
- Extremely high luminosity allows precision and correlation studies
- Low energies enhance access to TMD and nonperturbative effects
  - This greatly complements jet measurements from LHC, RHIC, etc.
  - Can use Belle II to constrain nonperturbative corrections to jet-functions etc.
- These points allow to measure effects not previously accessible in  $e^+e^-$ 
  - e.g. hadron or di-hadron correlation studies
- Relevance for EIC, understanding hadronization
  - Testing existing jet and TMD calculations in clean environment

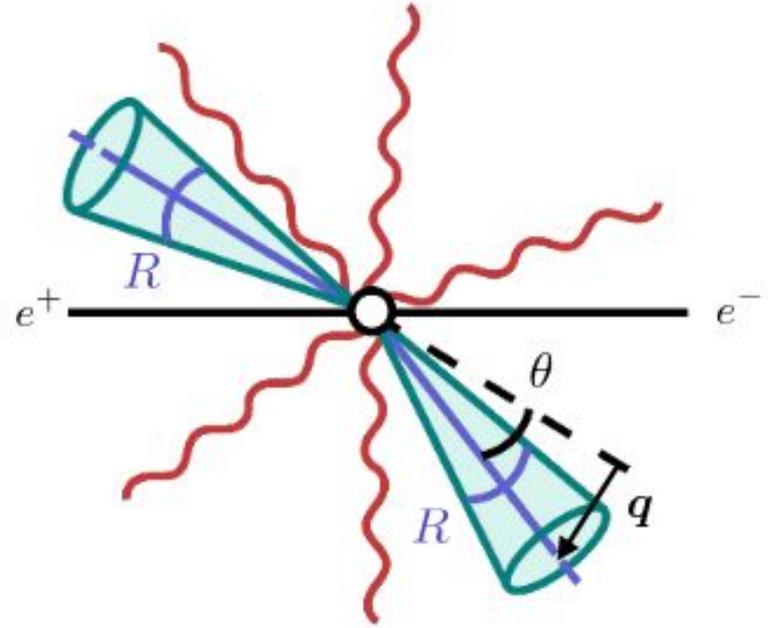
# Measuring jet $q_T$ spectrum at BELLE II: Definitions

Transverse momentum decorrelation  $\mathbf{q}$ :

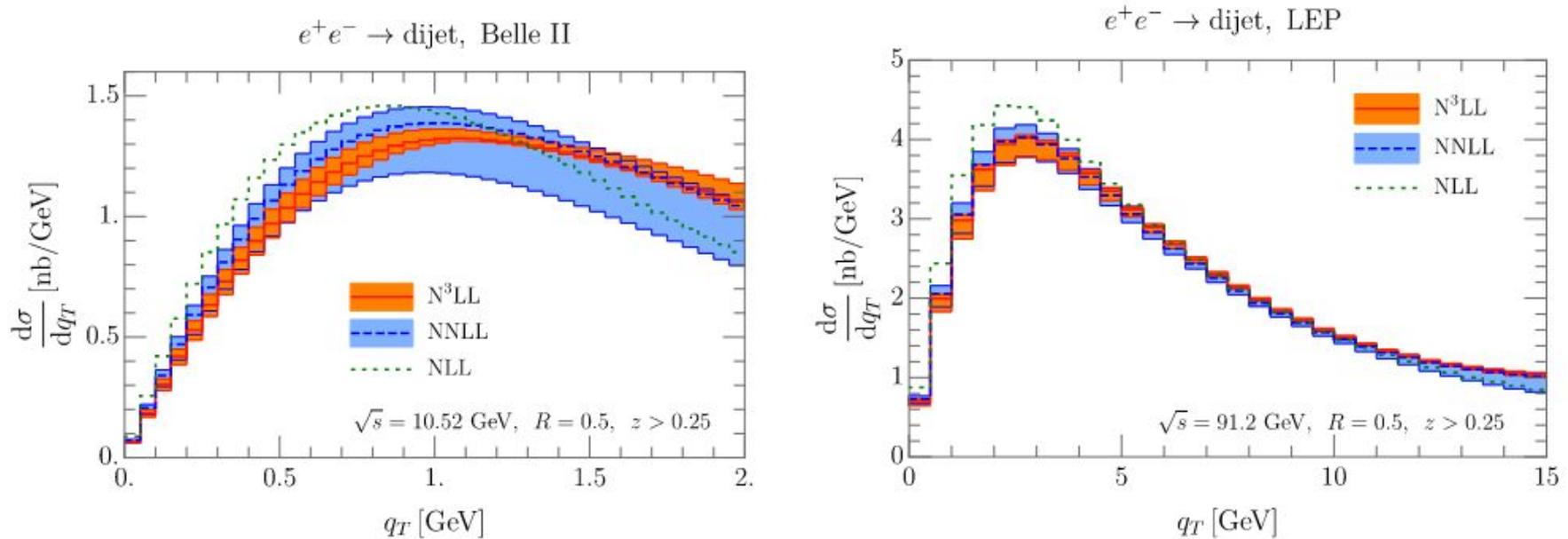
$$\mathbf{q} = \frac{\mathbf{p}_1}{z_1} + \frac{\mathbf{p}_2}{z_2}, \quad (e^+e^- \rightarrow \text{dijet})$$

$$q_T \equiv |\mathbf{q}| \ll \frac{\sqrt{s}}{2}$$

$$\theta = \arctan\left(\frac{2q_T}{\sqrt{s}}\right) \approx \frac{2q_T}{\sqrt{s}}$$



# Measuring jet $q_T$ spectrum at BELLE II



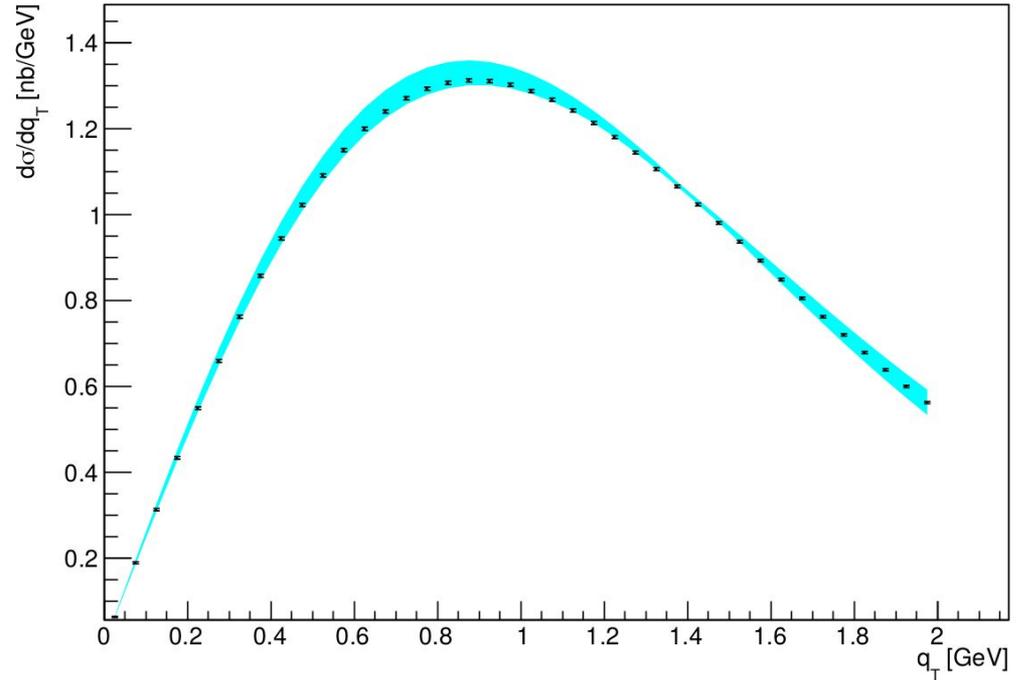
**Figure 5.** Perturbative convergence of the cross section differential in transverse momentum decorrelation, for Belle II (left) and LEP (right), for jet radius  $R = 0.5$  and jet energy fraction  $z > 0.25$ . The N<sup>3</sup>LL result is obtained with the prescription in eq. (6.1). The bands encode the perturbative uncertainty, as described in the text.

# Measuring jet $q_T$ spectrum at BELLE II

We know we have enough large enough datasets at Belle II

Predicted **statistical** uncertainties with  $10 \text{ fb}^{-1}$

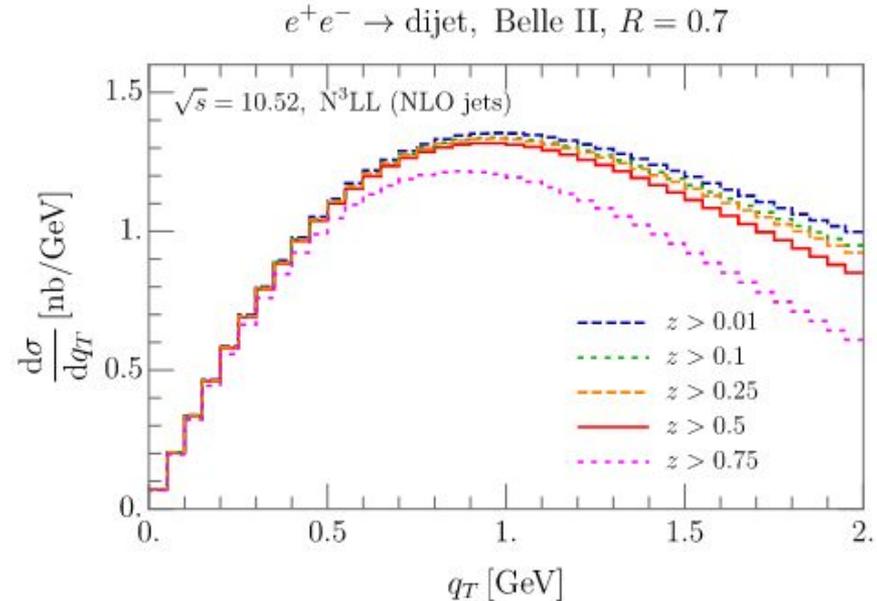
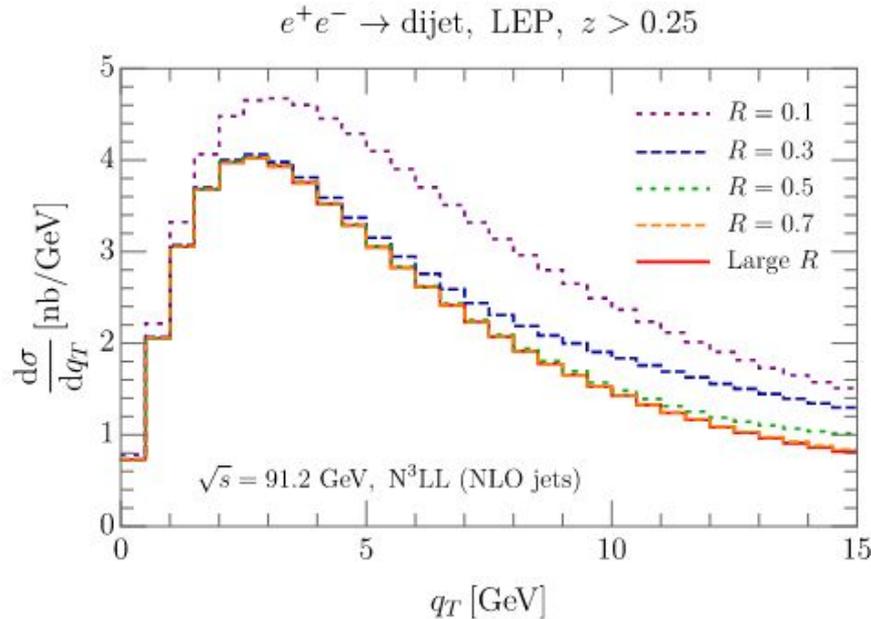
based on MC:



# Systematic Uncertainties

- Main task is to constrain systematic uncertainties
- We expect contributions from:
  - Imperfect detector response
  - Inhomogeneous detector noise
  - Non  $q\bar{q}$  contributions to dijet-sample (e.g. tau pairs)
  - Initial state radiation (ISR) makes effective CMS energy uncertain
- Similar to experience from previous Belle analyses

# Can also check dependence on jet radius R and jet z cut

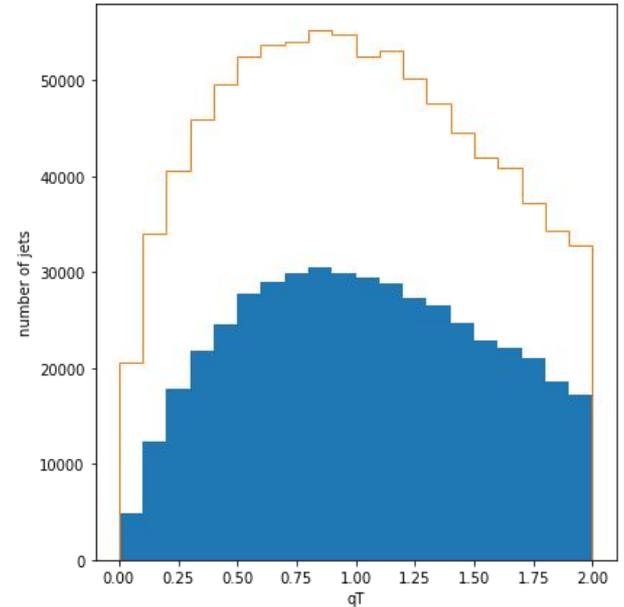
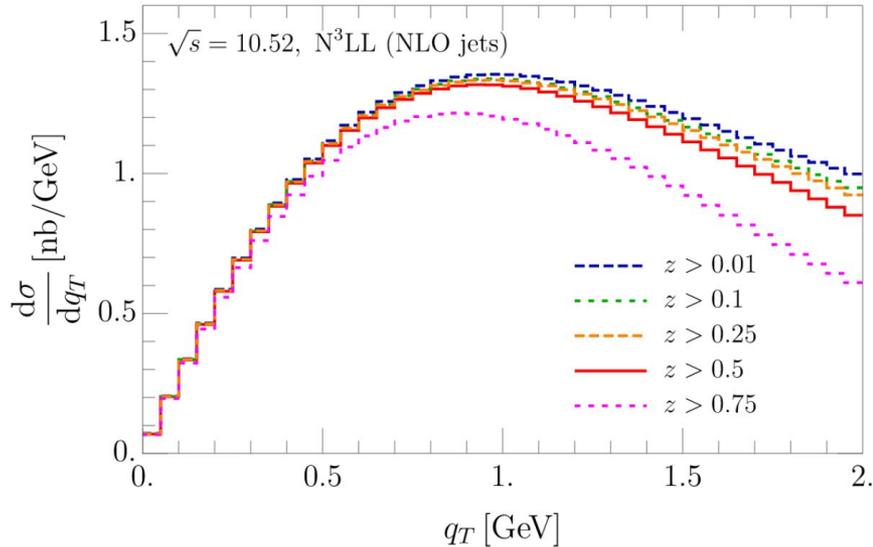


# Current Status

Spectrum close to being comparable, lacks unfolding and some corrections

(preliminary plot on right produced from uubar MC file)

$e^+e^- \rightarrow \text{dijet}$ , Belle II,  $R = 0.7$



# More possible measurements

- Many other jet-related observables can constrain QCD dynamics
  - help understand limits of perturbative QCD
  - constrain nonperturbative quantities
- Some examples:
  - hadron-in-jet fragmentation
  - energy-energy correlators
  - momentum sharing fraction  $z_g$
  - jet charge
  - flavor correlations
  - jet pull
  - jet angularities
  - T-odd effects
- See also:
  - “Opportunities for precision QCD physics in hadronization at Belle II -- a snowmass whitepaper” e-Print: 2204.02280 [hep-ex]

# Conclusions

- Majority of jet physics results are from high energy hadron collisions
- Belle data had been used for QCD and jet measurements
- Belle II electron-positron collisions provide clean environment for further hadronization/QCD studies
- Testing predictions across a wide energy range to gain confidence in theory
- Belle II is set to produce large dataset with good detector capabilities
- Measurement of the  $q_T$  spectrum serves as test of this extension to lower energies
- Possibility to test additional observables

# Backup slides and notes

# Physics Motivation and Goals

- We are interested in nucleon structure, described by PDFs
- We hope to extract PDFs from SIDIS at the EIC with increased precision
- Complication in SIDIS: both initial- and final-state non-perturbative physics
  - Final state non-perturbative physics can be extracted from  $e+e-$  data
- Jet observables offer some significant advantages over conventional ones
  - Put simply, replacing fragmentation functions with new “jet functions”

# Transverse momentum dependent distributions in $e^+e^-$ and semi-inclusive deep-inelastic scattering using jets

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**Daniel Gutierrez-Reyes,<sup>a</sup> Ignazio Scimemi,<sup>a</sup> Wouter J. Waalewijn<sup>b,c</sup> and Lorenzo Zoppi<sup>b,c</sup>**

<sup>a</sup>*Departamento de Física Teórica, Universidad Complutense de Madrid (UCM) and IPARCOS, E-28040 Madrid, Spain*

<sup>b</sup>*Institute for Theoretical Physics Amsterdam and Delta Institute for Theoretical Physics, University of Amsterdam, Science Park 904, 1098 XH Amsterdam, The Netherlands*

<sup>c</sup>*Nikhef, Theory Group, Science Park 105, 1098 XG, Amsterdam, The Netherlands*

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[L.Zoppi@uva.nl](mailto:L.Zoppi@uva.nl)

# Physics Motivation and Goals

- We are interested in the structure of the proton
- We hope to extract PDFs from SIDIS at the EIC with increased precision
- Complication in SIDIS: both initial- and final-state non-perturbative physics
- In SIDIS, replacing nonperturbative TMD FFs with calculable jet functions increases sensitivity to initial state nonperturbative physics
- Jet functions receive nonpert. corrections for small transverse momenta
- Because of jet functions' universality (nonpert. structure), can use  $e^+e^-$  data

*“[...] data from  $e^+e^-$  collisions could be used to fit a model for nonperturbative corrections to the jet function to be later applied to SIDIS”*

# Main results of paper by Gutierrez-Reyes et al.

- Proposal: measure jets instead of hadrons
  - Replacing TMD FFs with (new) TMD jet functions
  - When using WTA (winner-take-all), can use same factorization formulae
- Calculated Jet functions at one-loop level
- Phenomenological results for  $e^+e^-$  and SIDIS ( $q_T$ -spectra)
  - two-loop jet functions for large R limit  $\rightarrow$   $N^3$ LL accuracy
  - large R limit describes full R results well

# The $q_T$ measurement in practice

- Choosing data sets
- Event cuts: Selection of  $e^+e^- \rightarrow$  dijet events
  - e.g. require two highest energy jets to have  $E > 3.75$  GeV ( $z > 0.71$ )
- Finding appropriate track cuts / particle selection
  - photon energy cuts to avoid detector noise (e.g.  $E > 0.1$  GeV)
- Choice of jet definition and recombination scheme
  - $e^+e^-$  anti  $k_t$  algorithm, WTA
- Determining detector effects
  - Find response matrix with MC study and unfolding
- Study R and z-cut dependence of  $q_T$  spectrum
- Study systematic effects

# What datasets to use?

- Can use both on- and off-resonance
  - Gutierrez-Reyes et al. calculated for  $\sqrt{s} = 10.52$  GeV
    - Variation between dataset types expected smaller than ISR corrections
  - Ideally, proper dijet selection criteria are able to use the appropriate events from any set
  - If sufficient quantity, off-resonance could be easier to correct
- Use respective equivalent MC for unfolding (ideally 5-10 times as much data)

# Selection of $e^+e^- \rightarrow$ dijet events

- Currently selected by requiring that two highest energy jets have  $E > 3.75$  GeV each ( $z > 0.713$ )
  - This kinematically ensures that there can't be a third jet of similar energy
- See examples of selected and rejected events:

# Track cuts / particle selection

- Using standard quality cuts and PID
  - Currently using the most-likely particle lists provided in basf2
  - photons,  $\pi^+$ ,  $K^+$ , protons, electrons, muons and respective anti-particles
- Photon cut in E to remove noise
  - Currently require photons to be  $E > 0.1$  GeV
  - If not removed this could falsely add energy to the jets
  - This can be refined to detector-area specific cut-offs

# Jet definitions

- Gutierrez-Reyes et al. calculate  $q_T$  spectra for anti- $k_t$  with WTA
- Starting with this choice, perhaps comparing later

# Jet definitions (for $e^+e^-$ )

c.f. fastjet documentation  
section 4

## 4.5 Generalised $k_t$ algorithm for $e^+e^-$ collisions

FastJet also provides native implementations of clustering algorithms in spherical coordinates (specifically for  $e^+e^-$  collisions) along the lines of the original  $k_t$  algorithms [25], but extended following the generalised  $pp$  algorithm of [14] and section 4.4. We define the two following distances:

$$d_{ij} = \min(E_i^{2p}, E_j^{2p}) \frac{(1 - \cos \theta_{ij})}{(1 - \cos R)}, \quad (9a)$$

$$d_{iB} = E_i^{2p}, \quad (9b)$$

for a general value of  $p$  and  $R$ . At a given stage of the clustering sequence, if a  $d_{ij}$  is smallest then  $i$  and  $j$  are recombined, while if a  $d_{iB}$  is smallest then  $i$  is called an “inclusive jet”.

For values of  $R \leq \pi$  in eq. (9), the generalised  $e^+e^-$   $k_t$  algorithm behaves in analogy with the  $pp$  algorithms: when an object is at an angle  $\theta_{iX} > R$  from all other objects  $X$  then it forms an inclusive jet. With the choice  $p = -1$  this provides a simple, infrared and collinear safe way of obtaining a cone-like algorithm for  $e^+e^-$  collisions, since hard well-separated jets have a circular profile on the 3D sphere, with opening half-angle  $R$ . To use this form of the algorithm, define

```
JetDefinition jet_def(ee_genkt_algorithm, R, p);
```

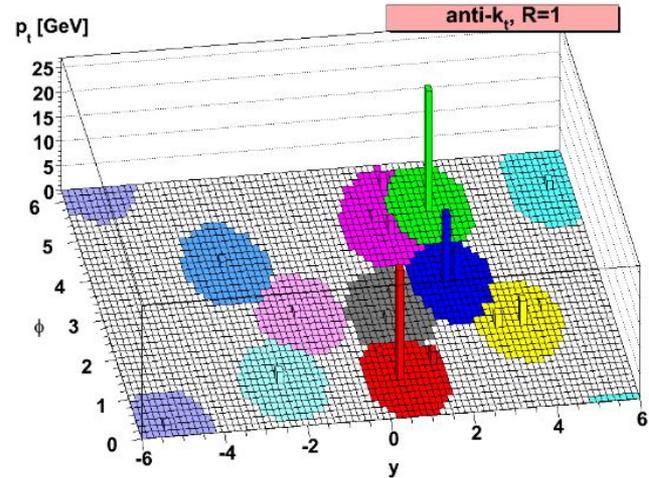
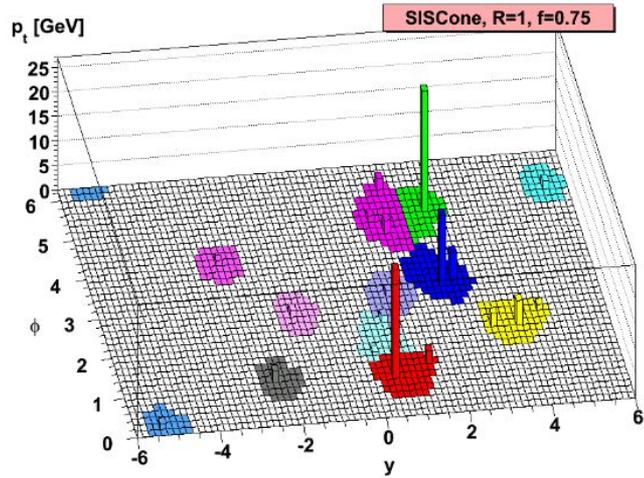
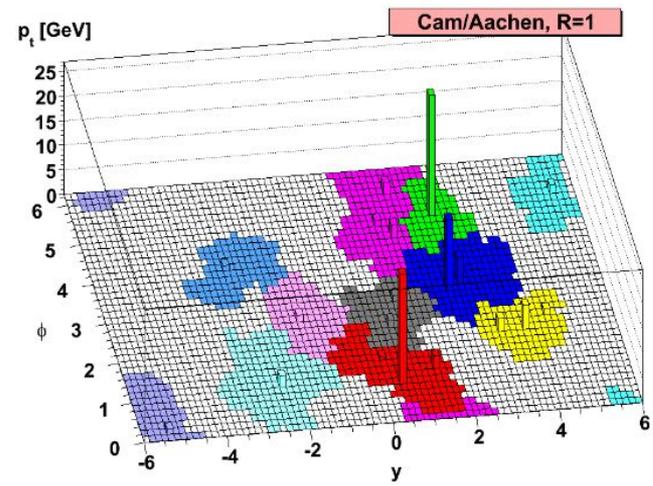
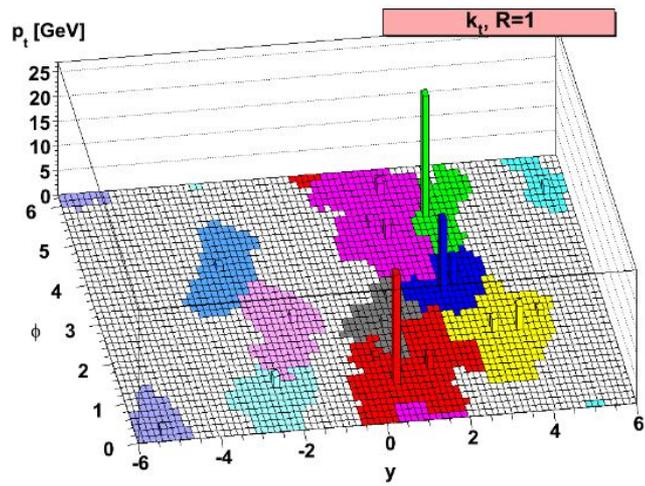
## 4.6 $k_t$ algorithm for $e^+e^-$ collisions

The  $e^+e^-$   $k_t$  algorithm [25], often referred to also as the Durham algorithm, has a single distance:

$$d_{ij} = 2 \min(E_i^2, E_j^2)(1 - \cos \theta_{ij}). \quad (10)$$

Note the difference in normalisation between the  $d_{ij}$  in eqs. (9) and (10), and the fact that in neither case have we normalised to the total energy  $Q$  in the event, contrary to the convention adopted originally in [25] (where the distance measure was called  $y_{ij}$ ). To use the  $e^+e^-$   $k_t$  algorithm, define

```
JetDefinition jet_def(ee_kt_algorithm);
```



# Difference between WTA and E-scheme recombination

- SJA simply sums 4-vectors
- WTA replaces two particles with massless particles moving in direction of more energetic particle, with new energy being the sum of both particles
  - Momentum of completed jet is parallel to momentum of most energetic constituent

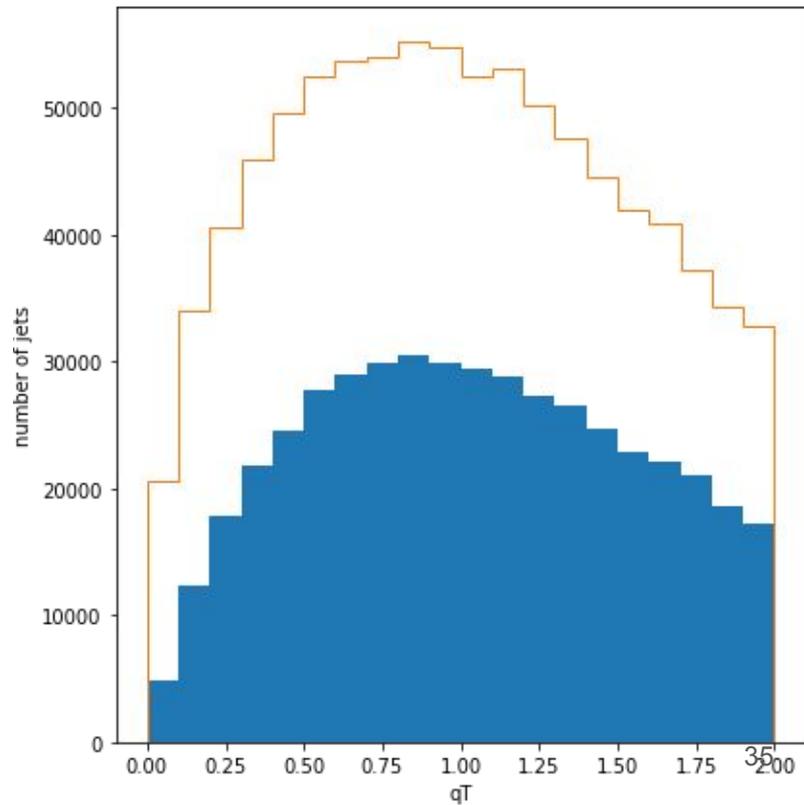
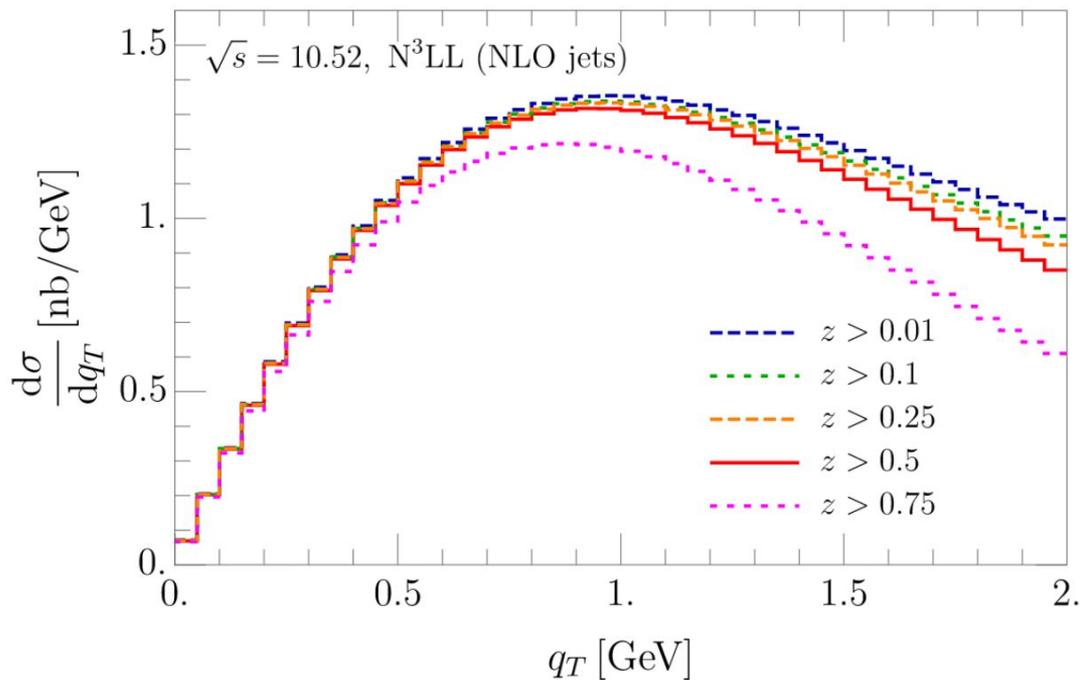
$$\text{SJA : } E_{(12)} = E_1 + E_2, \quad \vec{p}_{(12)} = \vec{p}_1 + \vec{p}_2,$$

$$\text{WTA : } E_{(12)} = E_1 + E_2, \quad \vec{p}_{(12)} = E_{(12)} \left[ \frac{\vec{p}_1}{|\vec{p}_1|} \theta(E_1 - E_2) + \frac{\vec{p}_2}{|\vec{p}_2|} \theta(E_2 - E_1) \right]$$

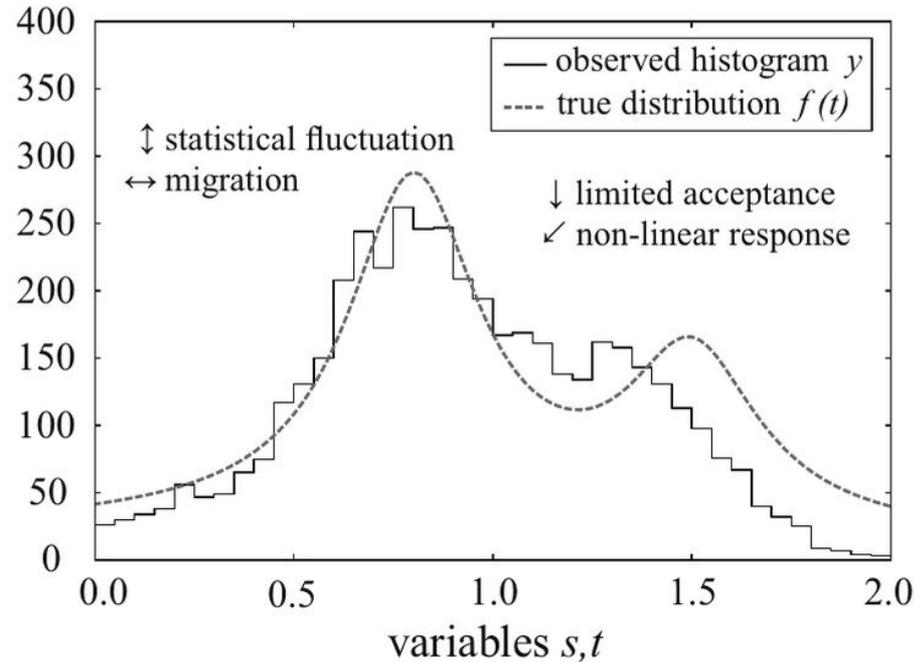
# Close to comparable, lacks unfolding

(plot on right produced from uubar MC file)

$e^+e^- \rightarrow \text{dijet}$ , Belle II,  $R = 0.7$



# Unfolding



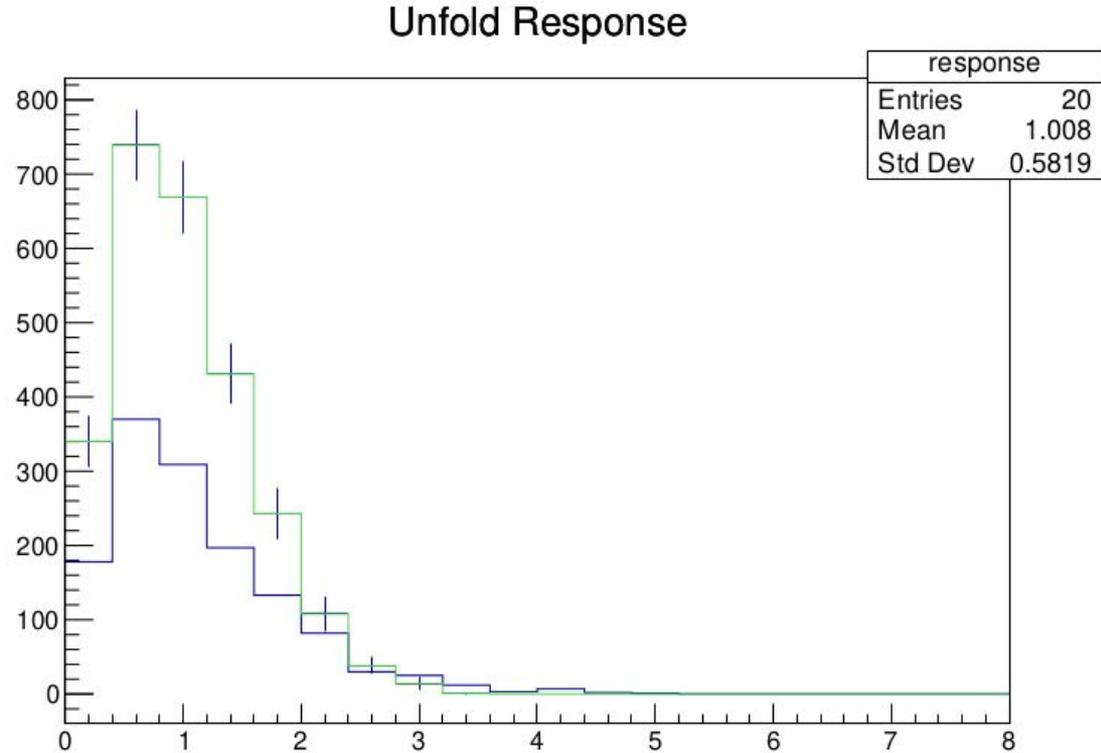
Multiple effects to consider:

- statistical fluctuations
- horizontal migration
- limited detector acceptance
- “non-linear response”
- additional backgrounds

**Figure 6.1** Illustration of the unfolding problem. The true distribution  $f(t)$  of a variable  $t$  to be measured in a particle physics experiment is shown. A corresponding simulated measurement  $g(s)$  is shown as histogram  $y$ . See the text for further details.

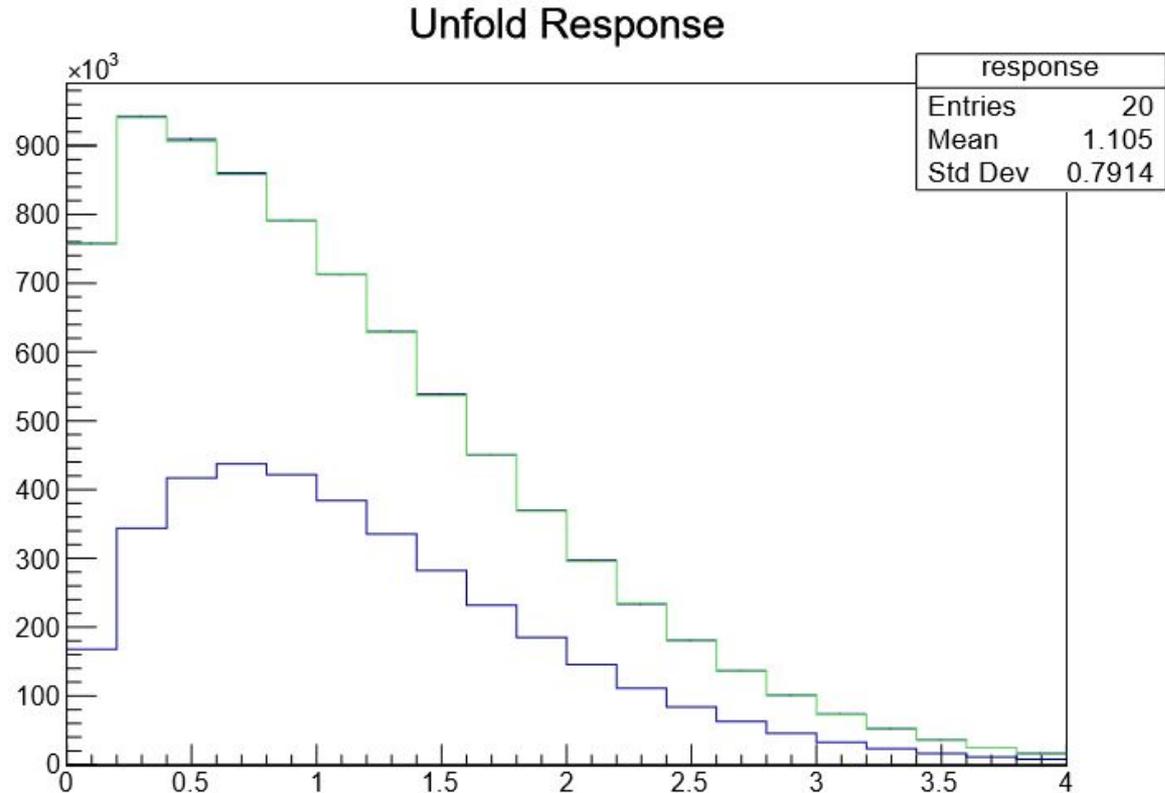
# Unfolding

- First a simple check:
  - Use same sample for response and unfolding
  - Bayes Unfolding (4 iterations)
  - AntiKt test file



# On larger (uubar) MC sample

Closure tests check out

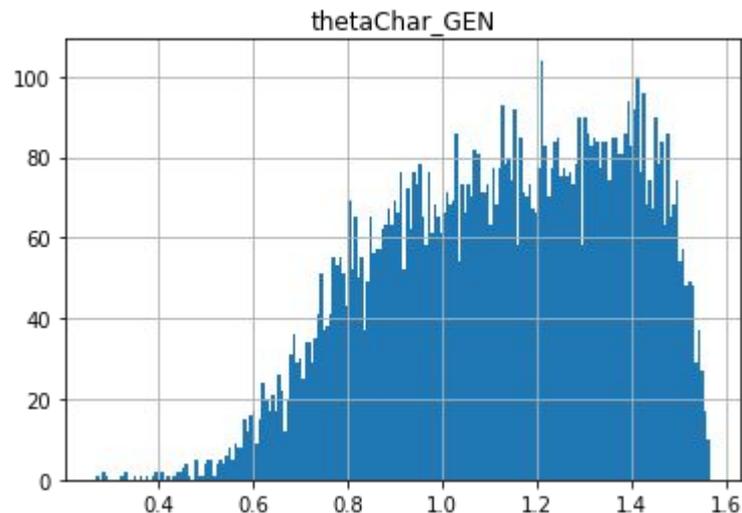
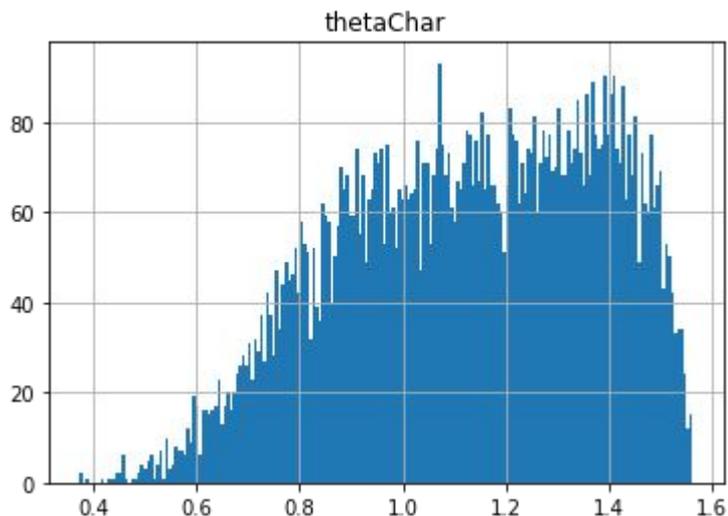


# Unfolding in polar angle

- Detector response is expected to depend on the orientation of the dijet
- Need to find a quantity to represent this orientation
  - e.g. thrust angle, one of the jet axes, etc.
- Implemented (unweighted) average angular distance from beam line of the two dominant jets

# Unfolding in polar angle

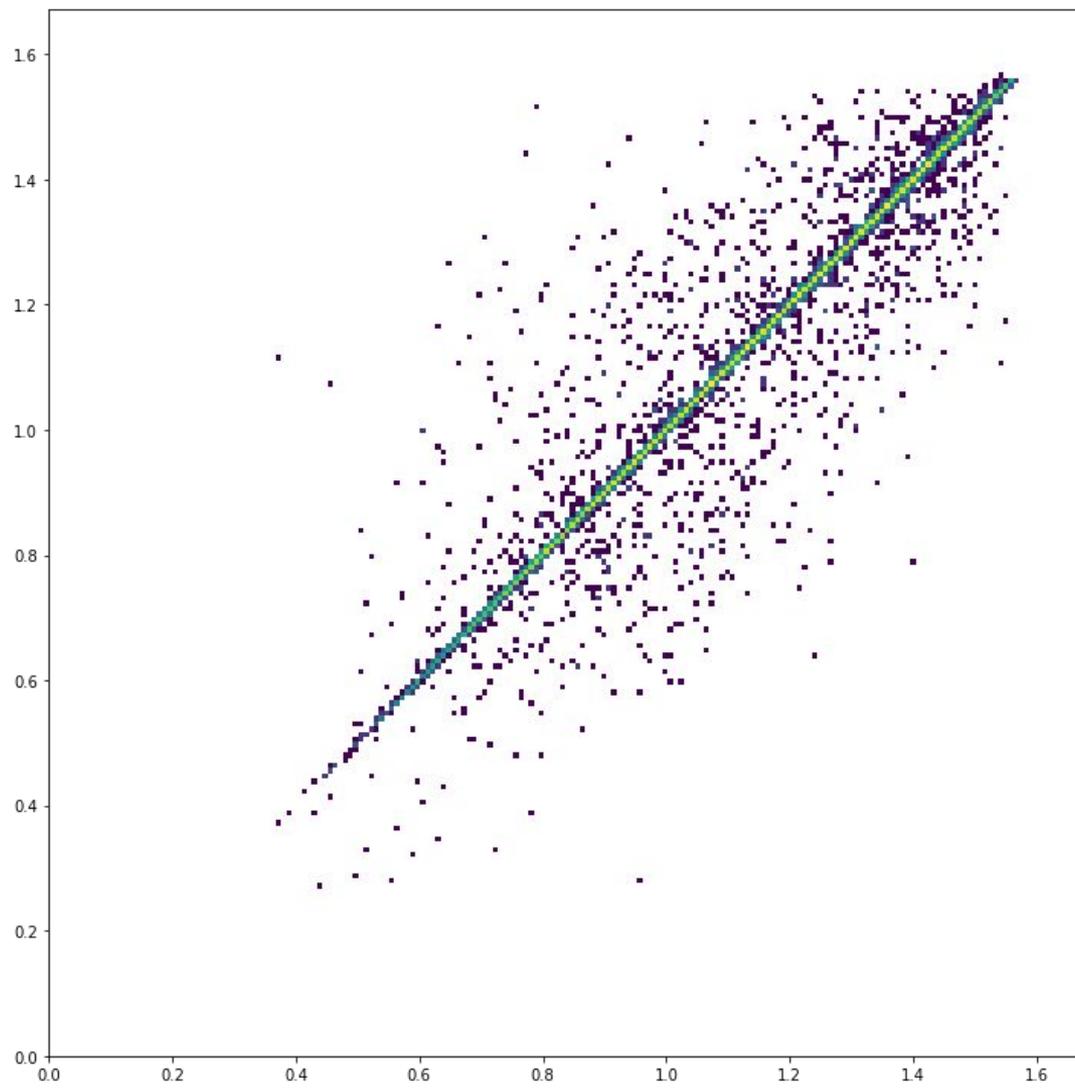
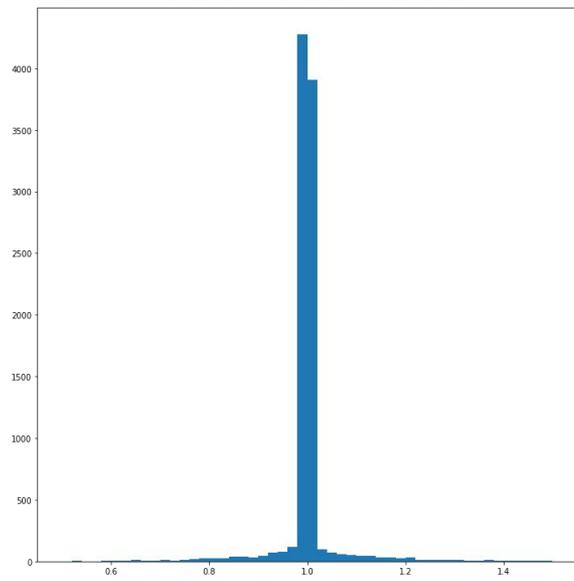
- This quantity is very similar between truth and reconstructed dijet events that pass dijet event cut



x-axis: reconstructed

y-axis: generated

below: ratio recon/truth



# Non qqbar corrections

Different event types have different cut-efficiencies

Checked how many events pass the 3.75 GeV cut-off for dijet selection

- BBbar events highly suppressed

	uubar	ddbar	ssbar	cbar	charged	mixed	taupair
MC truth	0.497	0.457	0.328	0.264	0.00864	0.00584	0.0809
MC reconstructed	0.101	0.0888	0.0629	0.0538	0.0035	0.00231	0.0327

# Current status

- Can calculate  $q_T$  from given event (in data and MC)
- Code is set up to compare MC truth with reconstructed
- Built event visualization to check and compare jet-clustering and event-selection
- Working on the unfolding procedure

## The Time-reversal Odd Side of a Jet

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<sup>3</sup>*Guangdong Provincial Key Laboratory of Nuclear Science, Institute of Quantum Matter,  
South China Normal University, Guangzhou 510006, China*

<sup>4</sup>*Guangdong-Hong Kong Joint Laboratory of Quantum Matter,  
South China Normal University, Guangzhou 510006, China*

We re-examine the jet probes of the nucleon spin and flavor structures. We find for the first time that the time-reversal odd (T-odd) component of a jet, conventionally thought to vanish, can survive due to the non-perturbative fragmentation and hadronization effects. This additional contribution of a jet will lead to novel jet phenomena relevant for unlocking the access to several spin structures of the nucleon, which were thought to be impossible by using jets. As examples, we show how the T-odd constituent can couple to the proton transversity at the Electron Ion Collider (EIC) and can give rise to the anisotropy in the jet production in  $e^+e^-$  annihilations. We expect the T-odd contribution of the jet to have broad applications in high energy nuclear physics.

The azimuthal asymmetry takes the general form [48]

$$R^{J_1 J_2} = 1 + \cos(2\phi_1) \frac{\sin^2 \theta}{1 + \cos^2 \theta} \frac{F_T(q_T)}{F_U(q_T)}, \quad (9)$$

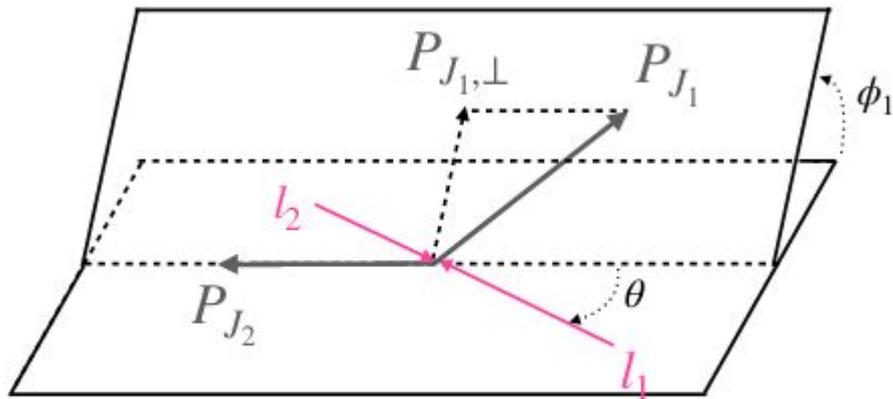


FIG. 4. Kinematics in the  $e^+e^-$  annihilation.

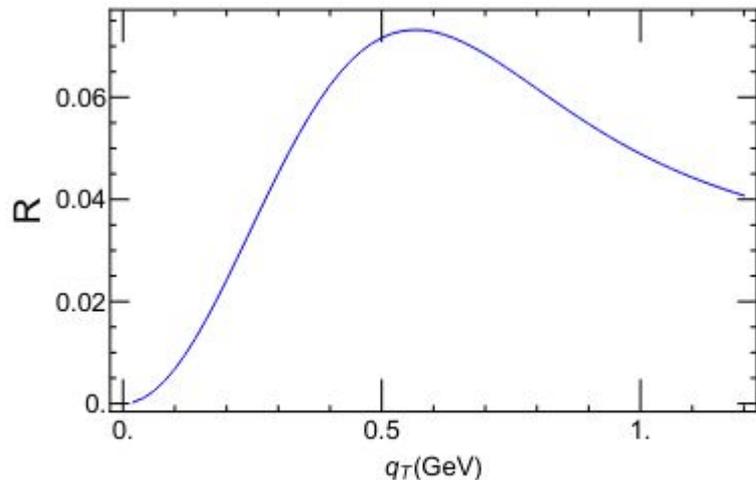


FIG. 5. Azimuthal asymmetry induced by the T-odd jets as a function of  $q_T$  in  $e^+e^-$ .

In Fig. 5, we present a prediction for the azimuthal asymmetry  $R = 2 \int d \cos \theta \frac{d\phi_1}{\pi} \cos(2\phi_1) R^{J_1 J_2}$  with  $\sqrt{s} = \sqrt{110} \text{ GeV}$ . We can see a non-vanishing azimuthal asymmetry induced by the T-odd jet. The actual magnitude and shape of this asymmetry should be determined by upcoming experimental data analyses. Similar azimuthal anisotropy can also be shown to exist in the dijet production in both  $pp$  and heavy ion collisions, whose studies will be investigated in the future.

# T-odd jets: measurement in practice

- Dijet event selection with similar criteria as for  $q_T$  spectrum
- Extracting  $\varphi_1$ ,  $\theta$ , and  $q_T$  for each event
- For selected  $q_T$  bin, fit distribution of  $\varphi_1$  values
  - Simply average over  $\theta$ , or use  $\theta$  bins?
- Fit is then comparable with calculations for  $R^{J_1 J_2} = 1 + \cos(2\phi_1) \frac{\sin^2 \theta}{1 + \cos^2 \theta} \frac{F_T(q_T)}{F_U(q_T)}$ ,
- What systematic problems are to be expected?
  - Angle  $\varphi_1$  problematic at low  $q_T$ ?

# A Fragmentation Approach to Jet Flavor

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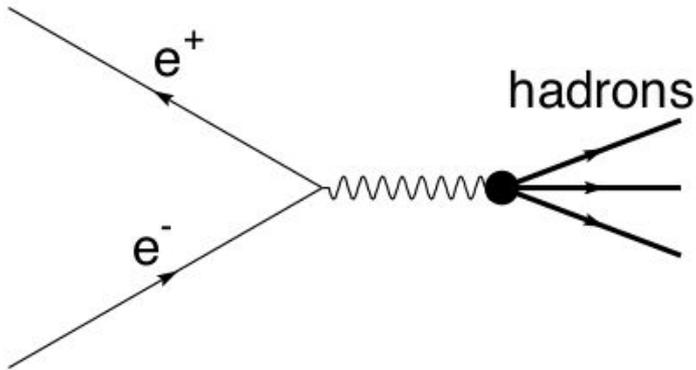
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**ABSTRACT:** An intuitive definition of the partonic flavor of a jet in quantum chromodynamics is often only well-defined in the deep ultraviolet, where the strong force becomes a free theory and a jet consists of a single parton. However, measurements are performed in the infrared, where a jet consists of numerous particles and requires an algorithmic procedure to define their phase space boundaries. To connect these two regimes, we introduce a novel and simple partonic jet flavor definition in the infrared. We define the jet flavor to be the net flavor of the partons that lie exactly along the direction of the Winner-Take-All recombination scheme axis of the jet, which is safe to all orders under emissions of soft particles, but is not collinear safe. Collinear divergences can be absorbed into a perturbative fragmentation function that describes the evolution of the jet flavor from the ultraviolet to the infrared. The evolution equations are linear and a small modification to traditional DGLAP and we solve them to leading-logarithmic accuracy. The evolution equations exhibit fixed points in the deep infrared, we demonstrate quantitative agreement with parton shower simulations, and we present various infrared and collinear safe observables that are sensitive to this flavor definition.

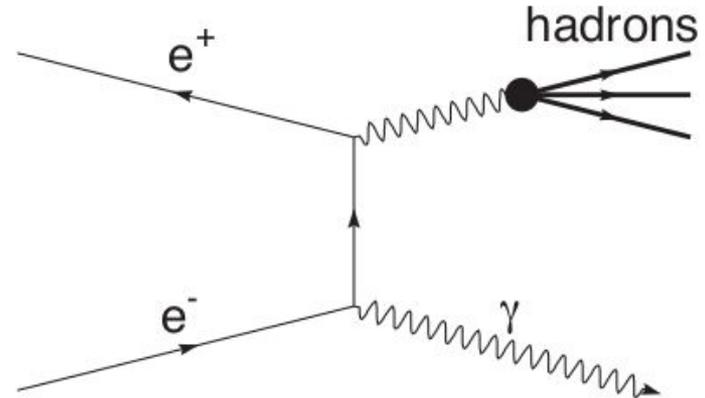
arXiv:2205.01117

# Selection of $e^+e^- \rightarrow$ dijet events: ISR effects

- Currently selected by requiring that two highest energy jets have  $E > 3.75$  GeV each ( $z > 0.713$ )
- Noticed contamination from events that look like ISR or only photons in MC



**Figure 21.2.1.** The lowest-order Feynman diagram describing the process of  $e^+e^-$  annihilation into hadrons.



**Figure 21.2.2.** The lowest-order Feynman diagram describing the process of  $e^+e^- \rightarrow \gamma_{\text{ISR}} + \text{hadrons}$ .